

States of Matter and Eudiometry

SOLUTIONS

EXERCISE - O

1. **Ans. (C)**
Gases do not have definite shape and volume. Their volume is equal to the volume of the container.
2. **Ans. (A)**
In gases, molecular attraction is very less and intermolecular spaces are large hence kinetic energy of gases is highest.
3. **Ans. (B)**
Barometer is used to measure atmospheric pressure of mixture of gases. Stagliometer is used to measure surface tension. Only manometer is used to measure pressure of pure gas in a vessel.
4. **Ans. (D)**
The mass of gas can be determined by weighing the container, filled with gas and again weighing this container after removing the gas. The difference between the two weights gives the mass of the gas.
5. **Ans. (C)**

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\frac{22.4}{273} = \frac{30.6}{373}$$
6. **Ans. (B)**
Using Charle's law
The correct order of pressure is
 $P_1 > P_2 > P_3$
7. **Ans. (A)**

$$V_2 = \frac{T_2}{T_1} \cdot V_1 = \frac{270\text{K}}{300\text{K}} \cdot 400\text{cm}^3 = 360\text{cm}^3$$

contraction = $V_1 - V_2 = 400 - 360 = 40\text{cm}^3$
8. **Ans. (A)**

$$P = \frac{\text{Constant}}{V}$$
9. **Ans. (C)**
At constant volume
 $P_I > P_{II} > P_{III} \Rightarrow T_I > T_{II} > T_{III}$
10. **Ans. (B)**
(A) $PV = nRT$
At constant temperature
 $PV = K$ ($T = \text{constant}$)
Higher the value of PV , higher the temperature.
So, $T_3 > T_2 > T_1$

Since, $P_1 = P_2 = P_3$

So, $V \propto T \Rightarrow V_3 > V_2 > V_1$

$$d = \frac{PM}{RT}$$

Since, $P_1 = P_2 = P_3$

$$d \propto \frac{1}{T} \Rightarrow d_1 > d_2 > d_3$$

(B) From Graph,

$V_3 > V_2 > V_1$ and $T_1 = T_2 = T_3$

Higher the volume, lesser the pressure because temperature is same for all.

$P_1 > P_2 > P_3$

$$d = \frac{PM}{RT}$$

Since, $T_1 = T_2 = T_3$

So, $d \propto P \Rightarrow d_1 > d_2 > d_3$

(C) From the graph,

$P_3 > P_2 > P_1$ and $T_1 = T_2 = T_3$

Higher the pressure, lesser the volume because temperature is same for all.

$V_1 > V_2 > V_3$

$$d = \frac{PM}{RT}$$

Since, $T_1 = T_2 = T_3$

So, $d \propto P \Rightarrow d_3 > d_2 > d_1$

(D) From the graph,

$d_3 > d_2 > d_1$ and $P_1 = P_2 = P_3$

$$d = \frac{PM}{RT} \Rightarrow d \propto \frac{1}{T}$$

So, $T_1 > T_2 > T_3$

$PV = nRT$

Since, $P_1 = P_2 = P_3$

$V \propto T$

So, $V_1 > V_2 > V_3$

11. **Ans. (D)**

$$P_{N_2} = \frac{\text{mol of } N_2}{\text{total mol}} \times \text{total pressure}$$

$$P_{N_2} = \frac{\frac{56}{28}}{\frac{56}{28} + \frac{96}{32}} \times 10 = \frac{2}{2+3} \times 10 = 4 \text{ atm}$$

$$P_{O_2} = 10 - 4 = 6 \text{ atm}$$

12. **Ans. (A)**

Initially $0.63 \times 1.2 = n_{He} RT$

after opening valve

$$P_{\text{He}} \times (1.2 + 3.4) = n_{\text{He}} RT$$

$$P_{\text{He}} = \frac{0.63 \times 1.2}{4.6} = 0.164 \text{ atm.}$$

13. **Ans. (D)**

$$\text{Rate of diffusion} \propto \frac{1}{\sqrt{\text{Molar mass}}}$$

CH_4 has lowest molar mass among all so its rate of diffusion faster.

14. **Ans. (B)**

$$r_{\text{Diffusion}} \propto \frac{1}{\sqrt{\text{Molar mass}}} ; r_{\text{Diffusion}} \propto \frac{1}{\sqrt{\text{density}}}$$

$$r_x = 3r_y$$

$$\frac{r_x}{r_y} = \sqrt{\frac{d_y}{d_x}}$$

$$\frac{3r_y}{r_y} = \sqrt{\frac{d_y}{d_x}} = \frac{d_x}{d_y} = \frac{1}{9}$$

15. **Ans. (A)**

$$r_{\text{Diffusion}} \propto \frac{n}{\sqrt{M}}$$

- Rate of diffusion in term of diffused mol

$$\frac{n_{\text{diffusion}}}{dt} \propto \frac{n}{\sqrt{M}}$$

$$\frac{\left(\frac{n_{\text{diffusion}}}{dt}\right)_{\text{He}}}{\left(\frac{n_{\text{diffusion}}}{dt}\right)_{\text{CH}_4}} = \frac{n_{\text{He}}}{n_{\text{CH}_4}} \times \sqrt{\frac{M_{\text{CH}_4}}{M_{\text{He}}}}$$

$$\frac{(n_{\text{diffusion}})_{\text{He}}}{(n_{\text{diffusion}})_{\text{CH}_4}} = \frac{4}{1} \times \sqrt{\frac{16}{4}} = \frac{8}{1}$$

16. **Ans. (D)**

$$\frac{r_{\text{O}_2}}{r_{\text{H}}} = \sqrt{\frac{M_{\text{H}_2}}{M_{\text{O}_2}}} = \sqrt{\frac{2}{32}} = \frac{1}{4}$$

$$\frac{n_{\text{O}_2}}{n_{\text{H}}} = \frac{1}{4} \quad \therefore n_{\text{H}} = 1 \text{ mole}$$

$$n_{\text{O}_2} = \frac{1}{4} \text{ mole}$$

$$\text{Mass of O}_2 = \frac{1}{4} \times 32 = 8 \text{ gm}$$

17. **Ans. (A)**

$$U_{\text{mp}} = \sqrt{\frac{2RT}{M}} ; U_{\text{avg}} = \sqrt{\frac{8RT}{\pi M}} ; U_{\text{rms}} = \sqrt{\frac{3RT}{M}}$$

$$U_{mp} : U_{rms} : U_{avg} = \sqrt{2} ; U_{avg} = \sqrt{\frac{8}{\pi}} ; U_{rms} = \sqrt{3} = 1 : 1.128 : 1.225$$

$$\frac{U_{rms}}{U_{av}} = 1.08$$

$$\frac{U_{av}}{U_{mp}} = 1.13$$

$$\frac{U_{rms}}{U_{mp}} = 1.225$$

18. **Ans. (C)**

At constant temperature KE remains constant.

19. **Ans. (A)**

At similar temperature KE of two gas are same.

20. **Ans. (D)**

$$\begin{aligned} U_{rms} &= \sqrt{\frac{U_1^2 + U_2^2 + U_3^2 + U_4^2}{N}} \\ &= \sqrt{\frac{2^2 + 3^2 + 4^2 + 5^2}{4}} \\ &= \sqrt{\frac{54}{4}} = 3.67 \text{ cm/s} \end{aligned}$$

21. **Ans. (B)**

$$(U_{mp})_{O_2} = (U_{rms})_{N_2}$$

$$\left(\sqrt{\frac{2RT}{M}} \right)_{O_2} = \left(\sqrt{\frac{3RT}{M}} \right)_{N_2}$$

$$\sqrt{\frac{2RT}{32}} = \sqrt{\frac{3R \times 700}{28}}$$

$$T = 1200K$$

22. **Ans. (C)**

$$U_{rms} = \sqrt{\frac{3P}{d}}$$

$$\frac{(U_{rms})_{O_2}}{(U_{rms})_{H_2}} = \sqrt{\frac{d_{H_2}}{d_{O_2}}} = \sqrt{\frac{1}{16}} = \frac{1}{4}$$

23. **Ans. (A)**

$$U_{avg} = \sqrt{\frac{8RT}{\pi M}}$$

$$\frac{U_1}{U_2} = \sqrt{\frac{T_1}{T_2}}$$

$$\frac{0.3}{U_2} = \sqrt{\frac{300}{1200}}$$

$$U_2 = 0.6 \text{ m/sec.}$$

24. **Ans. (A)**

Collision frequency (Z) of a gas at a particular pressure decreases with the rise in temperature.

$$Z \propto \frac{1}{T^{3/2}}$$

25. **Ans. (A)**

$$Z_{11} = \frac{\sigma^2 \pi \bar{U}}{\sqrt{2}} \left(\frac{N}{V} \right)^2 = \frac{\sigma^2 \pi}{\sqrt{2}} \left(\frac{N}{V} \right)^2 \sqrt{\frac{8RT}{\pi M}}$$

$$Z_{11} = \frac{\sigma^2 \pi}{\sqrt{2}} \left(\frac{N}{V} \right)^2 \sqrt{\frac{8P}{\pi d}} ; \text{ for constant volume } N^* = \frac{N}{V} = \text{constant}$$

$$Z_{11} \propto \sqrt{P}$$

26. **Ans. (C)**

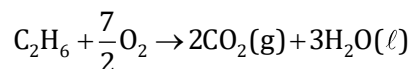
$$\lambda = \frac{1}{\sqrt{2} \pi \sigma^2 \left(\frac{N}{V} \right)}$$

$$\Rightarrow \frac{N}{V} = \frac{P \times N_A}{RT} = \frac{10^{-9} \times 6 \times 10^{23}}{1.01325 \times 0.0821 \times 300} = 2.4 \times 10^{13} \text{ molecules/L}$$

$$\Rightarrow 2.4 \times 10^{10} \text{ molecules/ml}$$

$$\Rightarrow \lambda = \frac{1}{1.44 \times \frac{22}{7} \times [500 \times 10^{-10}]^2 \times 2.4 \times 10^{10}} = 3.78 \times 10^3 \text{ cm}$$

27. **Ans. (B)**



V Ltr. 2V Ltr.

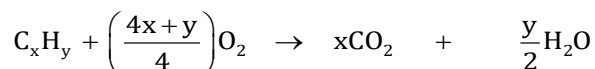


(3-V) 3(3-V) Ltr.

$$2V + 9 - 3V = 8 \text{ Ltr.}$$

$$V = 1 \text{ Ltr.}$$

28. **Ans. (D)**



$$10 \text{ ml} \quad 10x \quad \frac{10y}{2}$$

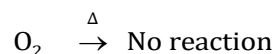
$$10x = 40 \quad \frac{10y}{2} = 50$$

$$x = 4$$

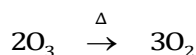
$$y = 10$$

The hydrocarbon is C_4H_{10}

29. **Ans. (B)**



x ml



$$(20 - x)\text{ml} \quad \frac{3}{2} (20 - x)\text{ml}$$

On passing from alkaline pyrogallol solution all the O_2 disappears.

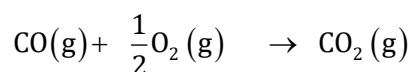
$$\frac{3}{2} (20 - x) + x = 29$$

$$60 - 3x + 2x = 58$$

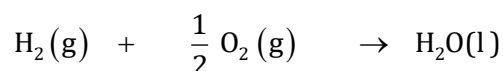
$$x = 2$$

$$\% \text{O}_2 \text{ in original mixture} = \frac{2}{20} \times 100 = 10\%$$

30. **Ans. (D)**



$$x \text{ ml} \quad \frac{x}{2} \text{ ml} \quad x \text{ ml}$$



$$(20 - x)\text{ml} \quad \left(\frac{20 - x}{2}\right)\text{ml} \quad -$$

Volume concentration = 23

$$\left(x + \frac{x}{2} + 20 - x + \frac{20 - x}{2}\right) - x = 23$$

$$\left(\frac{3x}{2} + 20 - x + 10 - \frac{x}{2}\right) - x = 23$$

$$30 - x = 23$$

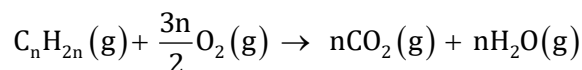
$$x = 7 \text{ ml}$$

$$V_{\text{CO}} = 7 \text{ ml}$$

$$V_{\text{H}_2} = 13 \text{ ml}$$

$$V_{\text{CO}} : V_{\text{H}_2} = 7 : 13$$

31. **Ans. (A)**



if there no volume changes i.e. $\Delta n_g = 0$

$$(n + n) - \left(1 + \frac{3n}{2}\right) = 0 \Rightarrow n = 2$$

32. **Ans. (D)**

'a' is related to attractive forces and 'b' to the volume of the molecules.

33. **Ans. (C)**

Greater the attractive force between molecules greater the value of 'a'

34. **Ans. (C)**

$$b \text{ is excluded volume or covolume} = b = 4 \times \frac{4}{3} \pi r^3 \cdot N_A$$

35. **Ans. (D)**

In an ideal gas there are no attractive or repulsive forces present. In real gas molecules intermolecular attractive forces are present.

36. **Ans. (D)**

$$\left(P + \frac{an^2}{V^2}\right)(V - nb) = nRT$$

37. **Ans. (C)**

At high pressure $a \simeq 0$

$$P(V - b) = RT$$

$$PV = Pb + RT$$

38. **Ans. (D)**

At low pressure and high temperature 'a' factor & 'b' factor become $\simeq 0$

39. **Ans. (A)**

$$\left(P + \frac{an^2}{V^2}\right)(V - nb) = nRT.$$

40. **Ans. (A)**

$$b = 4N_A V$$

41. **Ans. (A)**

At low pressure attractive force dominant, 'a' dominant and 'b' become negligible

$$\text{Hence } \left(p + \frac{a}{V^2}\right)(V - b) = RT$$

$$b \simeq 0$$

$$\left(p + \frac{a}{V^2}\right)V = RT$$

$$pV + \frac{a}{V} = RT \Rightarrow pV_m + \frac{a}{V_m} = RT$$

$$Z = \frac{pV_m}{RT} = 1 - \frac{a}{V_m RT}$$

$$\Rightarrow Z = \frac{pV_m}{RT} = 1 - \frac{a}{V_m RT}$$

42. **Ans. (D)**

$$(I) P(V - b) = RT$$

$$P = \frac{R}{(V - b)} \cdot T \Rightarrow \text{slope} = \frac{R}{V - b}$$

$$(II) PV - Pb = RT$$

$$V = \frac{RT}{P} + b \text{ slope} = \frac{R}{P} \text{ and intercept } b$$

$$(III) Z = \frac{PV}{RT} = 1 + \frac{Pb}{RT}; Z > 1$$

i.e., repulsive forces predominate.

43. **Ans. (C)**

$$Z = \frac{V_{\text{real}}}{V_{\text{ideal}}};$$

If $Z > 1$, $V_{\text{real}} > V_{\text{ideal}}$

$$Z = \frac{V_{\text{m,real}}}{V_{\text{m,ideal}}};$$

If $z > 1$

$$\Rightarrow V_{\text{m,real}} > V_{\text{m,ideal}}$$

repulsive forces are dominant and gases are difficult to compress.

If $Z < 1$, $V_{\text{real}} < V_{\text{ideal}}$;If $z < 1$

$$\Rightarrow V_{\text{m,real}} < V_{\text{m,ideal}}$$

attractive forces are dominant and gases are easy to compress.

44. **Ans. (D)**

Vander Waal's equation in virial form

$$Z = 1 + \frac{1}{V_{\text{m}}} \left(b - \frac{a}{RT} \right) + \frac{b^2}{V_{\text{m}}^2} + \frac{b^3}{V_{\text{m}}^3} \dots$$

Third virial coefficient $C = b^2$

$$b^2 = 4 \times 10^{-2}$$

$$b = \frac{0.2 \text{ l}}{\text{mol}} = 0.2 \text{ lit/mol}$$

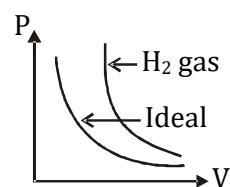
As $T > T_B$, so repulsive forces are dominant and $a \approx 0$

$$\left(P + \frac{an^2}{V^2} \right) (V - nb) = nRT$$

become $P(v - nb) = nRT$

$$1(V - 2 \times 0.2) = 2 \times 0.0821 \times 273$$

$$V = 45.3 \text{ l}$$

45. **Ans. (A)**For H_2 gas $+Z > 1$ 46. **Ans. (A)**

$$z = \frac{PV}{nRT} \Rightarrow \frac{Z_A}{Z_B} = \frac{P_A V_A}{P_B V_B} \Rightarrow \frac{3Z_B}{Z_B} = \frac{P_A \times 2V_B}{P_B \times V_B}$$

$$2P_A = 3P_B$$

47. **Ans. (D)**At low pressure when $T < T_b \Rightarrow Z < 1$

48. **Ans. (C)**

Greater the attractive force between gaseous molecules, greater the 'a', greater the liquification of gas.

49. **Ans. (A)**

$$T_c = \frac{8a}{27Rb}$$

Greater the T_c , greater the attractive force and greater the liquification of gas.

50. **Ans. (A)**

$$T_c = \frac{8a}{27Rb}$$

Due to very small size, attractive force between H_2 and He is negligible hence very small value of 'a' factor and critical temperature too.

51. **Ans. (C)**

Greater the attractive force between gaseous molecules, greater the 'a' greater the liquification of gas.

52. **Ans. (B)**

I. Slope of isotherm below critical point < 0 .

Slope of isotherm above critical point < 0 .

Slope of isotherm at critical point $= 0$.

So, slope of isotherm at critical point is maximum

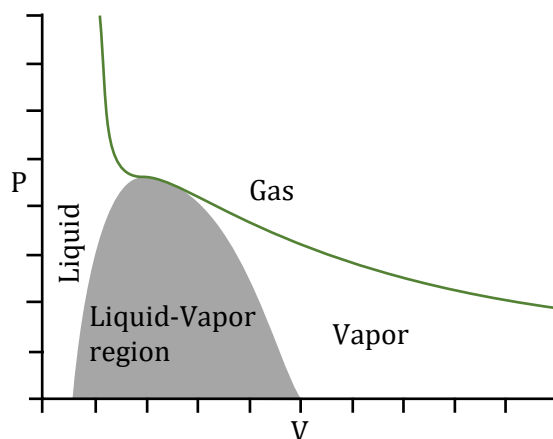
II. $T_c = \frac{8a}{27Rb}$

$$T_c \propto a$$

Larger value of T_c It means less decreases in temperature is required to liquify the gas. Gas will liquify at higher temperature. So, easier 'II' be liquification.

III. When gas is below critical temperature. It is 'liquid' so Vander Waal equation of state is not valid.

So, Answer (B)



53. **Ans. (D)**

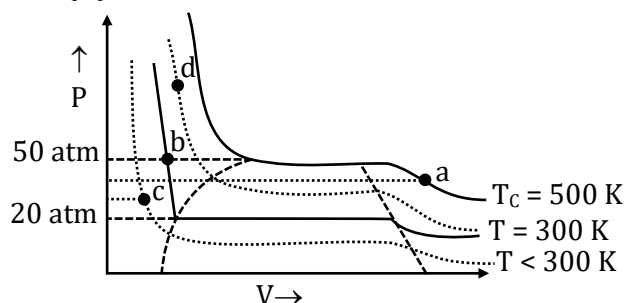
P_c , V_c and T_c are given hence 'a' and 'b' should be calculated using P_c and T_c as it is more reliable.

$$P_c = \frac{a}{27b^2}, T_c = \frac{8a}{27Rb}$$

$$\frac{P_c}{T_c} = \frac{R}{8b} \Rightarrow b = \frac{300 \times 1/12}{8 \times 50} = \frac{1}{16}$$

$$4 \times \frac{4}{3} \pi r^3 \cdot N_A = \frac{1}{16} \Rightarrow r = \left(\frac{3}{256 \pi N_A} \right)^{1/3}$$

54. **Ans. (D)**



- (a) at $T = 500 \text{ K}$, $P = 40 \text{ atm}$ corresponds to 'a' substance – gas
 (b) at $T = 300 \text{ K}$, $P = 50 \text{ atm}$ corresponds to 'b' substance – liquid
 (c) at $T < 300 \text{ K}$, $P > 20 \text{ atm}$ corresponds to 'c' substance – liquid
 (d) at $T < 500 \text{ K}$, $P > 50 \text{ atm}$ corresponds to 'd' substance – liquid
 So, Answer (D)

55. **Ans. (A,B,C)**

For Boyle's law

56. **Ans. (A,C,D)**

$$n_A = 3, n_B = 1, n_C = 1$$

$$(P_A)_i = \frac{n_A RT}{V} = \frac{3RT}{V}, (P_B)_i = \frac{n_B RT}{V} = \frac{1 \times RT}{V}$$

$$(P_A)_f = \frac{3RT}{V}, (P_B)_f = \frac{1 \times RT}{V}$$

$$(P_T)_i = \frac{(3+1)RT}{V} \Rightarrow (P_T)_f = \frac{5RT}{V} \Rightarrow \frac{(P_T)_i}{(P_T)_f} = \frac{4}{5}$$

$$\frac{P_1}{n_1} = \frac{P_2}{n_2} \Rightarrow \frac{20}{4} = \frac{P_2}{5}$$

$$P_2 = 25 \text{ atm} \quad (V = \text{constant as container is rigid})$$

$$\text{Partial pressure of C} = X_C \times P_T = \frac{1}{5} \times 25 = 5 \text{ atm.}$$

57. **Ans. (C,D)**

$$\lambda = \frac{1}{\sqrt{2} \pi \sigma^2 N^*}$$

$$N^* = \frac{N}{V} = \frac{PN_A}{RT}$$

$$\lambda = \frac{V}{\sqrt{2} \pi \sigma^2 N} = \frac{RT}{\sqrt{2} \pi \sigma^2 PN_A}$$

58. **Ans. (B,C,D)**

Liquefaction of gas not possible for $T > T_e$

$$T_b = \frac{a}{Rb}; T_c = \frac{8a}{27Rb}$$

EXERCISE - S

Ideal Gas

1. **Ans. (2)**

At bottom,

$$P_A = P_{\text{atm}} + P_{\text{Hg}} \\ = 1 + 1 = 2 \text{ atm}$$

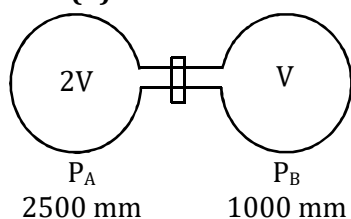
2. **Ans. (-111.5)**

Since P is constant, From Charles law,

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\frac{100}{323} = \frac{50}{T_2} = 161.5 \text{ K} \Rightarrow T_2 = -111.5^\circ\text{C}.$$

3. **Ans. (2)**



$$P_A \times 2V = (P_{\text{final}})_A \times (3V)$$

$$\frac{2}{3} \times 2500 = (P_{\text{final}})_A$$

$$P_{\text{total}} = \frac{5000}{3} + \frac{1000}{3} = 2000 \text{ mm or } = 2\text{m}$$

$$P_B \times V = (P_{\text{final}})_B \times 3V$$

$$\frac{1000}{3} = (P_{\text{final}})_B$$

4. **Ans. (0.028)**

$$P_{\text{H}_2\text{O}} = X_{\text{H}_2\text{O}} \times P_{\text{total}} = 0.0287 \times 0.977 = 0.028 \text{ bar}$$

5. **Ans. (1460)**

(Aqueous tension of $\text{H}_2\text{O} = 20 \text{ mmHg}$)

$$P_{\text{Total}} = P_{\text{O}_2} + P_{\text{H}_2\text{O}}$$

$$P_{\text{O}_2} (\text{initial}) = 740 - 20 = 720 \text{ mmHg}$$

$$(P_{\text{O}_2} V_{\text{O}_2})_{\text{initial}} = (P_{\text{O}_2} V_{\text{O}_2})_{\text{final}} \text{ (Boyle's law)}$$

$$720 \times V = P_{\text{O}_2} \times \frac{V}{2}$$

$$P_{\text{O}_2} = 1440 \text{ mm}$$

$$P_T = P_{\text{O}_2} + P_{\text{aq.}}$$

$$= 1440 + 20 = 1460 \text{ mm}$$

6. **Ans. (100)**

$$P = \frac{nR}{V} \cdot T \Rightarrow \log P = \log \frac{nR}{V} + \log T$$

$$Y = C + mx$$

$$\text{Intercept} = \log \frac{nR}{V} = 1$$

$$\frac{nR}{V} = 10$$

$$n = 10 \times \frac{V}{R} = \frac{10 \times 0.084}{0.084} = 100 \text{ mol}$$

7. **Ans. (0.347)**

$$\frac{r_A}{r_B} = \frac{n_A}{n_B} \cdot \sqrt{\frac{M_B}{M_A}} = \frac{w_A}{w_B} \left(\frac{M_B}{M_A} \right)^{3/2}$$

$$\Rightarrow \frac{r_A}{r_B} = \frac{1}{4} = \frac{2}{3} \left(\frac{M_B}{M_A} \right)^{3/2}$$

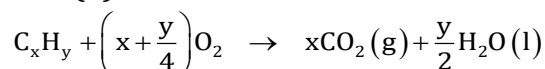
$$\left(\frac{M_A}{M_B} \right) = \left(\frac{8}{3} \right)^{2/3}$$

$$\frac{M_A}{M_B} = \frac{4}{(3)^{2/3}} = \frac{4}{(9)^{1/3}} = \frac{4}{2.08}$$

Let mass of gas A in the mixture be 2x and gas B be 3x

$$\frac{X_A}{X_B} = \frac{n_A}{n_B} = \frac{\frac{2x}{M_A}}{\frac{3x}{M_B}} = \frac{2}{3} \times \frac{2.08}{4} = 0.347$$

8. **Ans. (6)**



$$V \quad \left(x + \frac{y}{4} \right) V$$

$$\text{---} \quad \text{---} \quad V_x$$

$$\text{Volume contraction} = V_i - V_f$$

$$V_i = V + V \left(x + \frac{y}{4} \right)$$

$$V_f = Vx$$

$$2.5 V = V \left(1 + \frac{y}{4} \right)$$

$$y = 6$$

Number of H-atom in 1 molecule of hydrocarbon is 6.

9. **Ans. (9)**

$$Z_{11} \propto P^2 \text{ (at constant temperature)}$$

So, if pressure is tripled, Z_{11} increases by nine times.

10. **Ans. (1.256)**

$$Z = 1 - \frac{a}{V_m RT}$$

$$Z = \frac{PV_m}{RT} \Rightarrow V_m = \frac{RTZ}{P}$$

$$Z = 1 - \frac{a}{(RT)^2} \times \frac{P}{Z}$$

$$0.5 = 1 - \frac{a \times 100}{(273 \times 0.0821)^2 \times 0.5}$$

$$a = 1.256 \text{ atm L}^2 \text{ mol}^{-2}$$

11. Ans. (500)

At Boyle temperature real gas behave ideally

$$T_B = \frac{a}{Rb} = \frac{1.642}{0.0821 \times 0.04} = 500$$

12. Ans. (2)

$$4N \frac{4}{3} \pi r^3 = 3.2 \times \pi \times 10^{-6}$$

$$4 \times 6 \times 10^{23} \times \frac{4}{3} \pi r^3 = 3.2 \pi \times 10^{-6}$$

$$r^3 = 10^{-30} \text{ m}$$

$$r = 0.1 \text{ nm}$$

$$d = 2r = 0.2 \text{ nm}$$

13. Ans. (9)

$$\therefore Z_c = \frac{3}{8}; \frac{3}{8} = \frac{x}{24}; x = 3 \times 3; x = 9.$$

14. Ans. (0.36 & 0.00428)

$$T_c = 273 + 31 = 304 \text{ K}, P_c = 728 \text{ atm}$$

$$T_c = \frac{8a}{27Rb} \text{ and } P_c = \frac{a}{27b^2}$$

$$\therefore \frac{T_c}{P_c} = \frac{8a}{27Rb} \times \frac{27b^2}{a} = \frac{8b}{R}$$

$$\text{On substitution } \frac{304}{728} = \frac{8b}{0.082}$$

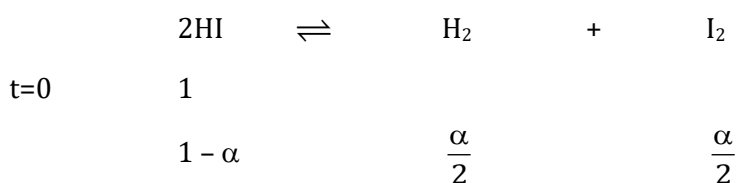
$$\therefore b = \frac{304 \times 0.082}{728 \times 8} = 4.28 \times 10^{-3} \text{ litre/mole}$$

$$\text{Now, } T_c = \frac{8a}{27Rb}$$

$$\therefore a = \frac{27RbT_c}{8} = \frac{27 \times 0.082 \times 4.28 \times 10^{-3} \times 304}{8} = 0.36 \text{ atm litre}^2 \text{ mole}^{-2}$$

15. Ans. (4.00)

$$d_{\text{Mixture}} = \frac{PM_{\text{mixture}}}{RT}$$



$$\text{Total moles} = 1 - \alpha + \frac{\alpha}{2} + \frac{\alpha}{2} = 1$$

$$M_{\text{mixture}} = \frac{\text{Total mass}}{\text{Total moles}} = \frac{128}{1}$$

$$d = \frac{1 \times 128}{0.08 \times 400} = 4 \text{ g/ml}$$

16. **Ans. ($T_3 = 360.00$, $T_4 = 90.00$, $P_1 = 5.00$, $P_2 = 1.50$, $V_1 = 16.00$)**

At point B $T_1 = 300 \text{ K}$

so, A to B is isothermal process

hence $(PV)_A = (PV)_B$

$$10 \times 4 = P_1 \times 8$$

$$P_1 = 5 \text{ atm}$$

Point B to C is isobaric process

$$\text{hence } \left(\frac{V}{T}\right)_B = \left(\frac{V}{T}\right)_C$$

$$\frac{8}{300} = \frac{V_1}{600}$$

$$V_1 = 16 \text{ liter}$$

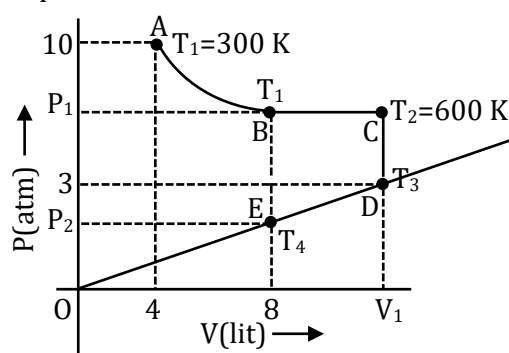
Point C to D is isochoric process

$$\text{hence } \left(\frac{P}{T}\right)_C = \left(\frac{P}{T}\right)_D$$

$$\frac{5}{600} = \frac{3}{T_3}$$

$$T_3 = 360 \text{ K}$$

At point E



observe that line joining D & E is straight & passing through origin slope of "OD" & ED are same

$$\text{so slope of } OD = ED = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\text{considering OD we get } \frac{V_1 - 0}{3 - 0} = m$$

$$\text{considering OE we get } \frac{8 - 0}{P_2 - 0} = m$$

$$\text{so } \frac{16}{3} = \frac{8}{P_2} \Rightarrow \boxed{P_2 = 1.5 \text{ atm}} \quad (V_1 = 16 \text{ liter})$$

point B & E are isochoric hence

$$\left(\frac{P}{T}\right)_B = \left(\frac{P}{T}\right)_E$$

$$\frac{5}{300} = \frac{1.5}{T_4}$$

$$T_4 = 90 \text{ K}$$

17. Ans. (a. (80.00), b. (1295.00))

(a) Given $P \propto r$ P = Pressure, r = radius

$$\text{so } \frac{P_1}{r_1} = \frac{P_2}{r_2}$$

given $P_1 = 1 \text{ atm}$ & $d_1 = 1 \text{ m}$ so $r_1 = 1/2 \text{ m}$

$P_2 = 3 \text{ atm}$ hence

$$\frac{P_1}{P_2} = \frac{r_1}{r_2} \Rightarrow r_2 = r_1 \times \frac{P_2}{P_1}$$

$$r_2 = \frac{1}{2} \times \frac{3}{1} = \frac{3}{2} \text{ m} \quad \left[\frac{r_2}{r_1} = 3 \right]$$

Assuming temperature to be constant as nothing is given about it.

$$\text{so } P_1 V_1 = n_1 RT$$

$$\& P_2 V_2 = n_2 RT$$

$$\text{or } \frac{P_1 V_1}{n_1} = \frac{P_2 V_2}{n_2}$$

Taking ballon to be perfect sphere

$$V_1 = \frac{4}{3} \pi r_1^3 \quad V_2 = \frac{4}{3} \pi r_2^3$$

$$P_1 = 1 \text{ atm} \quad P_2 = 3 \text{ atm}$$

$$n_1 = 1 \text{ mole} \quad n_2 = ?$$

$$\text{so } 1 \times \frac{4}{3} \pi r_1^3 = 3 \times \frac{4}{3} \frac{\pi r_2^3}{n_2}$$

$$\text{or } n_2 = 3 \left(\frac{r_2}{r_1} \right)^3$$

$$\text{putting } \frac{r_2}{r_1} = 3$$

$$n_2 = 3 \times (3)^3$$

$$= 81 \text{ moles}$$

so number of moles to be added

$$= n_2 - n_1 = 80 \text{ moles}$$

(b) If volume = 36π then

$$36\pi = \frac{4}{3} \pi r^3$$

$$\text{or } \Rightarrow r^3 = 27$$

$$r = 3 \text{ m}$$

now using the reaction

$$\frac{P_1}{r_1} = \frac{P_2}{r_2} \quad \text{calculated above}$$

$$P_2 = \frac{r_2}{r_1} \times P_1 \quad \text{Given } r_1 = 1/2$$

$$= 3 \times 2 \times 1 \quad r_2 = 3$$

$$P_2 = 6 \text{ atm} \quad P_1 = 1$$

so when pressure reaches 6 atm volume will become $36\pi\text{m}^3$; further filling the gas, will increase the volume, and balloon will get burst.

so again using

$$\frac{P_1 V_1}{n_1} = \frac{P_2 V_2}{n_2}$$

$$\text{where } P_1 = 1 \quad V_1 = \frac{4}{3} \pi r_1^3$$

$$n_1 = 1$$

$$P_2 = 6 \quad V_2 = 36\pi\text{m}^3$$

$$n_2 = ?$$

$$\frac{1 \times \frac{4}{3} \times \pi \times \left(\frac{1}{2}\right)^3}{1} = \frac{6 \times 36\pi}{n_2}$$

$$n_2 = \frac{6 \times 36\pi \times 3 \times 8}{4\pi}$$

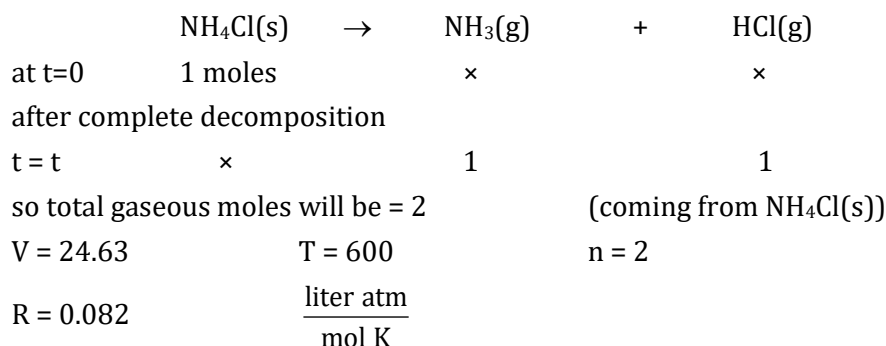
$$= 54 \times 24$$

$$n_2 = 1296$$

so, no. of moles to be added

$$= n_2 - n_1 = 1295 \text{ moles}$$

18. Ans. (i. (6.00), ii. (No))



using ideal gas equation

$$P = \frac{nRT}{V}$$

$$= \frac{2 \times 0.082 \times 600}{24.63}$$

$$P_{(\text{NH}_3 + \text{HCl})} = 4 \text{ atm}$$

Now lid was initially open so vessel has air at 1 atm & 300 k, when heated on closing the lid, the moles of air will remain same at T = 600 k

$$\left(\frac{P_1}{T_1} \right)_{\text{air}} = \left(\frac{P_2}{T_2} \right)_{\text{air}} \quad [\text{as Vessel volume is const.}]$$

$$\text{so } (P_2)_{\text{air}} = \frac{600 \times 1}{300} = 2 \text{ atm}$$

$$\text{hence } P_{\text{Total}} = p_{\text{air}} + p_{(\text{NH}_3 + \text{HCl})}$$

$$= 4 + 2 = 6 \text{ atm}$$

$$\text{Now } P_{\text{Inside}} = 6 \text{ atm}$$

$$P_{\text{outside}} = 1 \text{ atm}$$

$\Delta P = 5 \text{ atm}$; so lid will not blow

19. **Ans. (627.00)**

$$n = 1 \text{ mol}$$

$$P = \frac{1}{8.2} V$$

$$V = 8.2 P$$

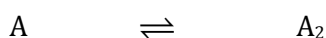
$$P_{\text{final}} = 3 \text{ atm}$$

$$T_f = \left(\frac{PV}{nR} \right)_f = \frac{P_f \times 8.2 \times P_f}{nR}$$

$$= \frac{3 \times 8.2 \times 3}{1 \times 0.082} = 900 \text{ k}$$

$$= 900 - 273 = 627^\circ\text{C}$$

20. **Ans. (2.00)**



Given Total mass = 96 g

$$T = 273^\circ\text{C} = 546 \text{ k}$$

$$V = 33.6 \text{ L}$$

mass of dimer = 48g (50%)

$$n_{A_2} = \frac{48}{96} = \frac{1}{2} \text{ mole}$$

$$n_A = \frac{48}{48} = 1 \text{ mole}$$

Total gaseous mole = 1 + 0.5 = 1.5

Now from

$$P = \frac{nRT}{V}$$

$$= \frac{1.5 \times 0.082 \times 546}{33.6} = 2 \text{ atm}$$

21. Ans. (6.00)

Temperature & total moles of gas are constant so

$$(PV)_i = (PV)_f$$

$$30 \times 2 = P_f \times 5$$

$$P_f = 12 \text{ atm}$$

Now partial press of C

$$P_C = \text{Mole fraction of C} \times P_{\text{Total}}$$

$$= \frac{3}{6} \times 12 = 6 \text{ atm}$$

22. Ans. (2.00)

As gases are non-reacting

$$(n_{\text{He}})_{\text{initial}} + (n_{\text{Ne}})_{\text{initial}} + (n_{\text{Xe}})_{\text{initial}} = (n_{\text{He}})_{\text{final}} + (n_{\text{Ne}})_{\text{final}} + (n_{\text{Xe}})_{\text{final}}$$

$$\frac{1.5 \times 2}{RT} + \frac{4 \times 2.5}{RT} + \frac{1 \times 1}{RT} = \frac{P_f \cdot (2 + 4 + 1)}{RT} \quad \left(n = \frac{PV}{RT} \right)$$

$$3 + 10 + 1 = P_f \times 7$$

$$P_{\text{final}} = 2 \text{ atm}$$

23. Ans. (380.00)

mole ratio of N_2 and O_2 is 75 : 25

final Total pressure = 1560 torr

final total pressure is due to $\text{N}_{2(g)}$, $\text{O}_{2(g)}$ & vapour of H_2O

$$\therefore p_{\text{N}_2} + p_{\text{O}_2} + (p_{\text{H}_2\text{O}})_{\text{vap.}} = 1560$$

$$p_{\text{N}_2} + p_{\text{O}_2} + 40 = 1560$$

$$p_{\text{N}_2} + p_{\text{O}_2} = 1520 \text{ torr}$$

pressure ratio or N_2 and O_2 is same as mole ratio

$$\therefore p_{\text{O}_2} = \left(\frac{25}{25 + 75} \right) \times 1520 = 380 \text{ torr}$$

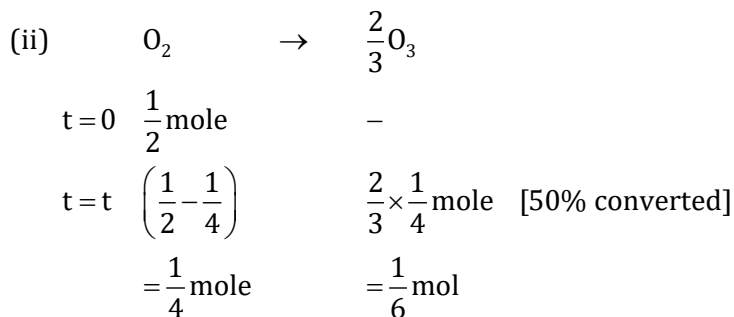
24. Ans. (i. (1.50), ii. (1.25), iii. (0.20 or 0.21))

$$(i) \frac{16}{32} = \frac{1}{2} \text{ mole of } \text{O}_2$$

$$\text{By } PV = nRT$$

$$P \times 8.2 = \frac{16}{32} \times 0.082 \times 300$$

$$= P = 1.5 \text{ atm}$$



By $PV = nRT$

$$\begin{aligned}
 P_{\text{Total}} &= \frac{n_{\text{Total}}RT}{V} \\
 &= \frac{5}{12} \times \frac{0.082 \times 300}{8.2} = 1.25 \text{ atm}
 \end{aligned}$$

(iii) At 50 k and 50% conversion

$$P_{\text{Total}} \times 8.2 = \left(\frac{1}{4} + \frac{1}{6}\right) \times 0.082 \times 50$$

$$P_{\text{Total}} = 0.208 \text{ atm}$$

25. **Ans. (7.00)**

$$V_{\text{Total}} = \frac{n_{\text{Total}}RT}{P}$$

$$n_{\text{Total}} = n_{\text{He}} + n_{\text{H}_2\text{O}}$$

$$n_{\text{H}_2\text{O}} = \left(\frac{PV_{\text{Total}}}{RT}\right)_{\text{H}_2\text{O}} = \frac{0.68 \times V_{\text{Total}}}{0.082 \times 273}$$

$$n_{\text{Total}} = 0.1 + \frac{0.68 \times V_{\text{Total}}}{0.082 \times 273}$$

$$n_{\text{Total}} = \left(0.1 + \frac{0.68 V_{\text{Total}}}{0.082 \times 273}\right) \times \frac{0.082 \times 273}{1}$$

$$V_{\text{Total}} = 2.24 + 0.68 V_{\text{Total}}$$

$$0.32 V_{\text{Total}} = 2.24$$

$$V_{\text{Total}} = \frac{2.24}{0.32} = 7 \text{ liter}$$

26. **Ans. (4.00)**

Initially $PV = nRT$

$$3 \times 24.6 = (n_{\text{D}_2} + n_{\text{H}_2}) \times 0.082 \times 300$$

$$3 = 1 + n_{\text{H}_2} \Rightarrow (n_{\text{H}_2})_i = 2 \text{ moles}$$

$$\text{Final mass ratio} = \frac{w_{\text{D}_2}}{w_{\text{H}_2}} = \frac{1}{4}$$

$$\left(\frac{n_{\text{D}_2}}{n_{\text{H}_2}}\right) = \frac{1/4}{4/2} = \frac{1}{8}$$

We know $\left(\frac{n_{D_2}}{n_{H_2}}\right)_f = \left(\frac{n_{D_2}}{n_{H_2}}\right) \cdot \left(\sqrt{\frac{M_{H_2}}{M_{D_2}}}\right)^n$

$$\frac{1}{8} = \frac{1}{2} \left(\sqrt{\frac{2}{4}}\right)^n \Rightarrow \frac{1}{4} = \left(\frac{1}{2}\right)^{\frac{n}{2}}$$

$$\Rightarrow n = 4 \text{ steps}$$

27. **Ans. (8.00)**

$$u_{av} = \sqrt{\frac{8RT}{\pi M}}$$

$$u_{rms} = \sqrt{\frac{3RT}{M}}$$

$$u_{av} = 1.84 \times 10^4 \text{ cm/sec}$$

$$= 184 \text{ m/sec}$$

$$\frac{u_{av}}{u_{rms}} = \sqrt{\frac{8}{3\pi}} = 0.92$$

$$u_{rms} = \left(\frac{184}{0.92}\right)$$

$$KE = \frac{1}{2} m \cdot (u_{rms})^2 \quad (\text{per molecule})$$

$$= \frac{1}{2} \times \frac{48 \times 10^{-3}}{6 \times 10^{23}} \times \left(\frac{184}{0.92}\right)^2$$

$$KE = 1.6 \times 10^{-21} \text{ J} = x$$

$$\therefore \left(\frac{x}{2} \times 10^{22}\right) = 8$$

28. **Ans. (i. (0.012 atm), ii. (2.50×10^{22}), iii. (3.60 J), iv. (300.00 J), v. ($1 : \sqrt{2}$), vi. (1 : 2500))**

(i) For container A

$$P = \frac{nRT}{V} = \frac{N}{N_A} \cdot \frac{RT}{V}$$

$$= \frac{6 \times 10^{20}}{6 \times 10^{23}} \times \frac{8 \times 300}{2 \times 10^{-3}} = 1200 \text{ Pa} = 0.012 \text{ atm}$$

(ii) For container B

$$P = \frac{nRT}{V} = \frac{N}{N_A} \cdot \frac{RT}{V}$$

$$N = \frac{PN_A V}{RT}$$

$$= \frac{10^5 \times 6 \times 10^{23} \times 2 \times 10^{-3}}{8 \times 600}$$

$$= 2.5 \times 10^{22}$$

(iii) For container A

$$KE_{\text{Total}} = \frac{3}{2} RT \times \text{No. of moles of ideal gas}$$

$$= \frac{3}{2} \times 8 \times 300 \times \frac{6 \times 10^{20}}{6 \times 10^{23}} = 3.6 \text{ J}$$

(iv) For container B

$$\begin{aligned} KE_{\text{Total}} &= \frac{3}{2} RT \times \text{No. of moles of ideal gas} \\ &= \frac{3}{2} \times 8 \times 600 \times \frac{2.5 \times 10^{22}}{6 \times 10^{23}} = 300 \text{ J} \end{aligned}$$

$$(v) \frac{(U_{\text{MPS}})_A}{(U_{\text{MPS}})_B} = \frac{\left(\sqrt{\frac{2RT}{M}} \right)_A}{\left(\sqrt{\frac{2RT}{M}} \right)_B} = \sqrt{\frac{T_A}{T_B}} = \sqrt{\frac{300}{600}} = \frac{1}{\sqrt{2}}$$

$$(vi) z_{11} = \frac{1}{\sqrt{2}} \pi \sigma^2 u_{\text{avg}} N^2$$

$$z_{11} = \frac{1}{\sqrt{2}} \pi \sigma^2 \sqrt{\frac{8RT}{\pi M}} \cdot \left(\frac{N}{V} \right)^2$$

$$z_{11} \propto \sqrt{T} \cdot (N)^2$$

$$\begin{aligned} \frac{(z_{11})_A}{(z_{11})_B} &= \sqrt{\frac{300}{600}} \times \left(\frac{6 \times 10^{20}}{2.5 \times 10^{22}} \right)^2 \\ &= \frac{1}{\sqrt{2}} \times \frac{36}{6.25 \times 10^4} \\ &= \frac{1}{2.45 \times 10^3} \approx \frac{1}{2.5 \times 10^3} = \frac{1}{2500} \end{aligned}$$

Real Gas

29. **Ans. (58.82)**

$$\text{Molar volume of mercury} = \frac{200}{13.6} \text{ cm}^3$$

$$\text{So, value of } b = \frac{200}{13.6} \times 4 = 58.82$$

30. **Ans. (0.50)**

$$PV = ZnRT$$

$$P = Z \frac{n}{V} RT$$

$$P = ZCRT$$

$$72 = Z(6)(.08 \times 300)$$

$$Z = 0.5$$

31. **Ans. (222.22)**

$$P(V - nb) = nRT$$

$$240 (10 - .08n) = n (.08) (300)$$

$$240 (10 - .08n) = 24 n$$

$$100 - 0.8n = n$$

$$n = \frac{100}{1.8} \Rightarrow \text{mass of He} = \frac{100}{1.8} \times 4 = 222.22 \text{ gm}$$

32. Ans. (1.68 or 1.69)

$$\text{Critical volume } V_c = \frac{\text{Molar mass}}{\text{Density}}$$

$$V_c = \frac{30}{0.4} \text{ cm}^3$$

$$V_c = 75 \text{ cm}^3$$

$$3b = 75$$

$$b = 25 \frac{\text{cm}^3}{\text{mol}} = .025 \frac{\text{Litre}}{\text{mol}}$$

$$T_c = \frac{10^4}{41}$$

$$\frac{8a}{27Rb} = \frac{10^4}{41}$$

$$\frac{8a}{27 \times .0821 \times .025} = \frac{10^4}{41}$$

$$a = 1.6875 \text{ atm L}^2 \text{ mol}^{-2}$$

33. Ans. (60.00)

$$T_b = \frac{a}{Rb} = \frac{4.10}{(.0821) \left(\frac{1}{6} \right)} = 300 \text{ K}$$

So at 300 K this gas will behave like a ideal gas.

$$PV = nRT$$

$$(.0821) V = 0.2 (.0821) (300)$$

$$V = 60 \text{ Litre}$$

34. Ans. (1.62)

$$\text{Mass of 1 litre gas} = 1.6 \text{ g} = \frac{1.6}{32} = \frac{1}{20} \text{ mol}$$

$$\left(P + \frac{an^2}{V^2} \right) (V - nb) = nRT$$

$$\left(P + \frac{4 \left(\frac{1}{20} \right)^2}{1^2} \right) \left(1 - \frac{1}{20} \times 0.4 \right) = \frac{1}{20} \times .08 \times 400$$

$$\left(P + \frac{1}{100} \right) (0.98) = 1.6$$

$$P = 1.62 \text{ atm}$$

EXERCISE - JEE (Advanced) PYQ

1. **Ans. (B)**

TIPS/Formulae :

Compressibility factor of ideal gas $(Z) = \frac{PV}{nRT}$

For one mole of ideal gas at STP

$$Z = \frac{P \times 22.4}{RT}$$

For other gases $Z < 1$ and $Z = \frac{P \times V_m}{RT}$

$$\therefore V_m < 22.4 \text{ litres}$$

Alternate solutions

$$(PV)_{\text{Observed}} / (PV)_{\text{Ideal}} < 1$$

$$\Rightarrow V_{\text{obs}} < V_{\text{ideal}}, V_{\text{obs}} < 22.4 \text{ litre.}$$

2. **Ans. (C)**

TIPS/Formulae :

$$U_{\text{rms}} = \sqrt{\frac{3RT}{M}}$$

$$\sqrt{\frac{3RT_{\text{H}_2}}{2}} = \sqrt{7} \sqrt{\frac{3RT_{\text{N}_2}}{28}};$$

$$\therefore T_{\text{N}_2} = 2T_{\text{H}_2} \text{ or } T_{\text{N}_2} > T_{\text{H}_2}$$

3. **Ans. (T)**

$$\rightarrow P \propto T$$

$$\rightarrow \text{collision frequency} \propto U_{\text{avg.}} \propto \sqrt{T}$$

4. **Ans. (D)**

$$U_{\text{RMS}} = \sqrt{\frac{3RT}{M}}$$

Using ideal gas equation

$$PV = RT = \frac{W}{M} RT \quad \frac{RT}{M} = \frac{PV}{w} = \frac{P}{d}$$

Where d is the density of the gas

$$\therefore U_{\text{RMS}} = \sqrt{\frac{3P}{d}} \text{ at constant pressure}$$

$$U_{\text{RMS}} \propto \frac{1}{\sqrt{d}}$$

option (d) is correct

5. **Ans. (434.17)**

IPS/Formulae :

$$C_{\text{rms}} = \sqrt{\frac{3RT}{M}}, C_{\text{av}} = \sqrt{\frac{8RT}{\pi M}}$$

$$\frac{C_{rms}}{C_{av}} = \sqrt{\frac{3RT}{M}} \times \sqrt{\frac{\pi M}{8RT}} = \sqrt{\frac{3\pi}{8}} = 1.085$$

$$C_{rms} = 1.085 \times C_{av} = 1.085 \times 400 = 434 \text{ ms}^{-1}$$

6. **Ans. (C)**

For positive deviation : $PV = nRT + nPb$

$$\Rightarrow \frac{PV}{nRT} = 1 + \frac{Pb}{RT}$$

Thus, the factor nPb is responsible for increasing the PV value, above ideal value, b is actually the effective volume of molecule. So, it is the finite size of molecules that leads to the origin of b and hence positive deviation at high pressure.

7. **Ans. (B)**

TIPS/Formulae :

Use Grahams' law of diffusion

$$\frac{r_{He}}{r_{CH_4}} = \sqrt{\frac{M_{CH_4}}{M_{He}}} = \sqrt{\frac{16}{4}} = 2$$

8. **Ans. (RT)**

The Vander Waal equation (for one mole) of a real gas is

$$\left(P + \frac{a}{V_m^2} \right) (V_m - b) = RT$$

$$PV_m - Pb + \frac{a}{V_m} - \frac{ab}{V_m^2} = RT$$

$$PV_m = RT + Pb - \frac{a}{V_m} + \frac{ab}{V_m^2} \quad \dots(i)$$

Note This step : To calculate the intercept $P \rightarrow 0$, hence $V_m \rightarrow \infty$ due to which the last two terms on the right side of the equation (can be neglected).

$$\therefore PV_m = RT + Pb$$

When $P = 0$, intercept = RT

9. **Ans. (B)**

For gas A, $a = 0$, $Z = 1 + \frac{Pb}{RT}$ implies Z varies linearly with pressure.

For gas B, $b = 0$, $Z = 1 - \frac{a}{VRT}$. Hence, Z does not vary linearly with pressure.

10. **Ans. (D)**

Matching

(A) $\rightarrow$ (P), (S)

[Because 200 atm pressure is very large for H_2 gas, at very high pressure $Z > 1$]

(B) $\rightarrow$ (R)

[Since $p \sim 0$ it means very low pressure so ideal behaviour is observed]

(C) $\rightarrow$ (P) & (Q)

[Since P is 1 atm, Z for CO_2 would be less than 1]

(D) $\rightarrow$ (R)

In real gas with very high molar volume, molecules will be very far apart from each other due to which Vander Waals forces as well as actual vol. occupied by molecule will be negligible.

11. **Ans. (A,C,D)**

(A), (C), (D) are correct

$$\left(P + \frac{n^2 a}{V^2}\right)(V - nb) = nRT$$

At low pressure, when the sample occupies a large volume, the molecules are so far apart for most of the time that intermolecular forces play no significant role, and the gas behaves virtually ideal

perfectly. a & b are characteristic of a gas and are independent of temp. The term $\left(P + \frac{n^2 a}{V^2}\right)$ represents

the pressure exerted by an ideal gas while P represents the pressure exerted by a real gas.

12. **Ans. (B)**

Correction factor for attractive force for n moles of real gas is given by the term mentioned in (b)

13. **Ans. (4)**

$$V_{\text{rms}} \text{ of } x = \sqrt{\frac{3RT_x}{M_x}}$$

$$V_{\text{mp}} \text{ of } y = \sqrt{\frac{2RT_y}{M_y}}$$

Given $V_{\text{rms}} = V_{\text{mp}}$

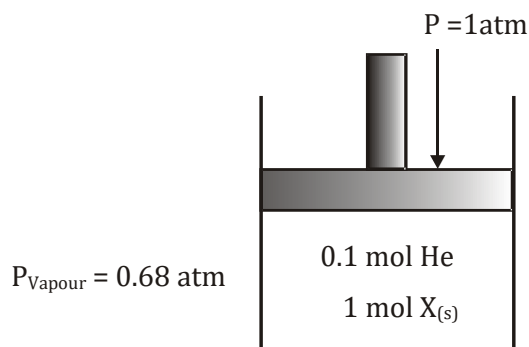
$$\Rightarrow \sqrt{\frac{3RT_x}{M_x}} = \sqrt{\frac{2RT_y}{M_y}}$$

$$\Rightarrow M_y = \frac{2RT_y M_x}{3RT_x} = \frac{2 \times 60 \times 40}{3 \times 400}$$

$$M_y = 4$$

14. **Ans. (7)**

Since external pressure is 1 atm



$$P_{\text{vapour}} + P_{\text{He}} = 1$$

$$\Rightarrow P_{\text{He}} = 1 - 0.68 = 0.32 \text{ atm}$$

Now from ideal gas equation $\Rightarrow PV = nRT$

$$\Rightarrow 0.32 \times V = 0.1 \times (R \times 273)$$

$$\Rightarrow V = 7 \text{ litre.}$$

15. **Ans. (C)**

$$\left(P + \frac{a}{V^2}\right)(V - 0) = RT \quad \text{as } (n = 1)$$

$$PV = RT - \frac{a}{V}$$

On comparing slope from graph

$$-a = \frac{20.1 - 21.6}{3 - 2}$$

$$-a = \frac{-1.5}{1} = a = 1.5$$

16. **Ans. (C)**

$$\left[\frac{d_x/t}{d_y/t} \right] = \sqrt{\frac{M_y}{M_x}}$$

$$\frac{d}{24-d} = \sqrt{\frac{40}{10}} = 2$$

$$d = 48 - 2d$$

$$d = 16 \text{ cm}$$

17. **Ans. (D)**

The experimental value of d is found to be smaller than the estimated, this is due to increased collision frequency of X with the inert gas as compared to that of Y with inert gas.

With increase in collision frequency, the molecular speed decreases then the expected so the distance converted will be less.

18. **Ans. (2.22)**

Finally

$$P_A = P_B, T_A = T_B$$

($\therefore$ Heat flow take place until temp. become equal)

$$\text{hence } = \frac{n_A}{V_A} = \frac{n_B}{V_B}$$

$$= \frac{5 \times 1}{R \times 400} = \frac{3 \times 1}{R \times 300}$$

$$\frac{V_A}{V_B} = \frac{5}{4}$$

$$V_A = \frac{5}{9} \times 4 = 2.22$$

($\therefore$ total value = 4l)

19. **Ans. (ABC)**

$$U_{\text{RMS}} \propto \sqrt{T}$$

$$KE_{\text{avg}} \propto T$$

20. **Ans. (B)**

Graph represents symmetrical distribution of speed and hence, the most probable and the average speed should be same. But the root mean square speed must be greater than the average speed.

JEE (Advanced) Practice Paper

1. **Ans. (B)**

$$V_1 = 5L \quad V_2 = 1L$$

$$P_1 = 1 \text{ bar} \quad P_2 = ?$$

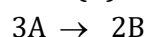
$$P_1 V_1 = P_2 V_2$$

$$1 \times 5 = P_2 \times 1$$

$$P_2 = 5$$

$$\% \text{ increase} = 400\%$$

2. **Ans. (B)**



$$1-\alpha \quad \frac{2}{3}\alpha$$

$$\text{Total moles} = 1 - \frac{\alpha}{3}$$

$$P = \frac{nR}{V} \cdot T$$

$$y = m \cdot x$$

↓

slope

$$\text{As per given data } \tan 42.95 = 0.8$$

$$\therefore \frac{nR}{V} = 0.8$$

$$\therefore n = \frac{0.8 \times 0.082}{0.082}$$

$$n = 0.8$$

$$\therefore 1 - \frac{\alpha}{3} = 0.8$$

$$\therefore \alpha = 0.6$$

3. **Ans. (C)**

Let the distance travelled by gas X at the point of meeting be "x"

Distance travelled by gas Y = "150 - x"

Applying Rate of diffusion equation.

$$\frac{r_X}{r_Y} = \frac{n_X}{n_Y} \sqrt{\frac{M_Y}{M_X}}$$

$$\Rightarrow \frac{\frac{x}{t}}{\frac{150-x}{t}} = \frac{3}{2} \sqrt{\frac{80}{20}}$$

$$\frac{x}{150-x} = 3$$

$$x = 450 - 3x \Rightarrow 4x = 450$$

$$x = 112.5 \text{ cm}$$

$$\text{Distance of A from Q} = 150 - x = 37.5 \text{ cm}$$

4. **Ans. (C)**

$$Z = \frac{PV}{nRT}$$

$$V = 0.064 \text{ L}$$

5. **Ans. (A)**

$$\text{Critical temperature} = \frac{8}{27} \frac{a}{Rb}$$

$$\frac{8}{27} \frac{a}{Rb} < 300 \quad [200 < T_c < 300]$$

$$\frac{a}{b} < 81$$

$$\frac{8a}{27Rb} > 200$$

$$\boxed{\frac{a}{b} > 54}$$

$$\left[54 < \frac{a}{b} < 81 \right]$$

6. **Ans. (C)**

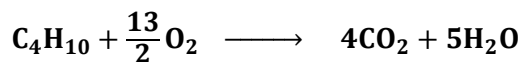
C₄H₁₀, CH₄ & CO mixture → **C₄H₁₀** 40% by volume

∴ **Volume of C₄H₁₀** = 80 ml

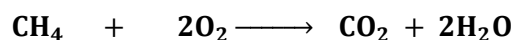
& **CH₄ & CO** volume = 120 ml

If **CH₄** volume = x ml

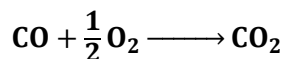
Volume of **CO** = 120 - x ml



$$80 \text{ ml} \qquad \qquad \qquad 4 \times 80 = 320 \text{ ml}$$



$$x \text{ ml} \qquad \qquad \qquad x \text{ ml}$$



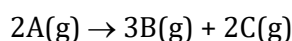
$$120 - x \qquad \qquad 120 - x \text{ ml}$$

$$\text{Total CO}_2 = 320 + 120 - x + x = 440 \text{ ml}$$

7. **Ans. (B,D)**

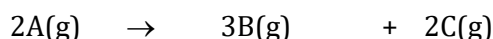
Since initially manometer shown no difference in mercury level therefore initial pressure of gas

A = 76 cm of Hg = 1 atm



$$\text{initial pressure (atm)} \quad 1 \qquad \qquad 0 \qquad \qquad 0$$

It is given that after sparking pressure of gas 'A' is decreased to 0.8 atm. It means 0.2 atm of 'A' is converted into B and C.



$$\text{pressure after sparking (atm)} \quad 1 - 0.2 = 0.8 \quad \left(\frac{3}{2} \times 0.2 = 0.3 \right) \quad 0.2$$

$$\therefore \text{After sparking } P_{\text{total}} = 0.8 + 0.3 = 1.1 \text{ atm.}$$

initially total pressure was 1 atm

$$\therefore \text{Difference in Hg level} = 0.3 \text{ atm} = 22.8 \text{ cm of Hg} \\ = 228 \text{ mm of Hg}$$

8. Ans. (A,B,C,D)

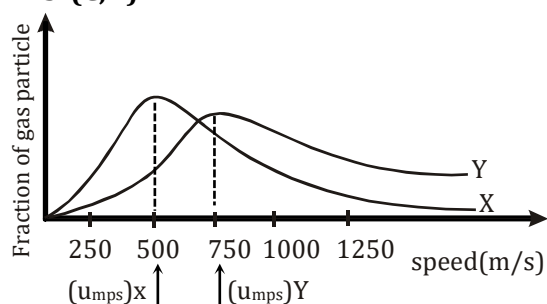
$$V = \frac{nRT}{P} : V_{H_2} = \frac{\left(\frac{1}{2}\right) \times 0.0821 \times (273 + 273)}{1} = 22.4 \ell$$

$$V_{He} = \frac{\left(\frac{2}{4}\right) \times 0.0821 \times (273 + 273)}{1} = 22.4 \ell$$

$$V_{CH_4} = \frac{\left(\frac{3}{16}\right) \times 0.0821 \times (273 + 273)}{1} = 8.4 \ell$$

$$V_{SO_2} = \frac{\left(\frac{4}{64}\right) \times 0.0821 \times (273 + 273)}{1} = 2.8 \ell$$

9. Ans. (C,D)



For option (A) From Fig (i), it is clear that $(u_{mps})Y > (u_{mps})X$

$$\text{or, } \sqrt{\frac{2RT}{M_Y}} > \sqrt{\frac{2RT}{M_X}}$$

since both X and Y are at same temp.

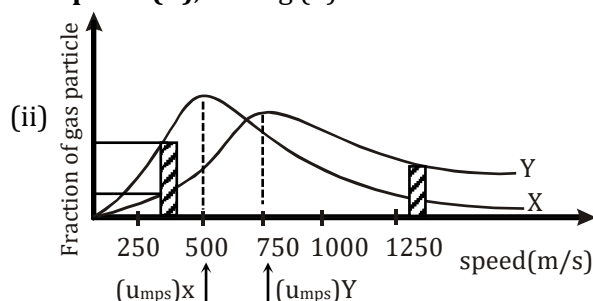
$$\therefore \boxed{M_Y < M_X} \quad \dots(1)$$

since X is CH_4 whose molar mass is 16.

$\therefore$ Y can't be CO_2 because. $M_{CO_2} = 44$

$\therefore$ (A) is wrong.

for option (B), see Fig (ii)



in lower speed region shaded area in figure, fraction of molecules of X > fraction of molecules of Y. As shaded area is greater for X as compared to Y. In higher speed region, shaded area in fig. fraction of molecules of Y > fraction of molecules of X. Therefore (B) is wrong.

for option 'C'

under identical conditions of P & T.

$$\text{rate of effusion} \propto \frac{1}{\sqrt{M}}$$

$$\therefore M_Y < M_X \text{ (from (i))}$$

$$\therefore \text{rate of effusion of Y} > \text{X.}$$

$$\therefore \text{(C) is correct.}$$

for option 'D'

$$\text{Molar KE} = \frac{3}{2}RT$$

$$\therefore \text{Both X and Y are at same temp.} = 200\text{K}$$

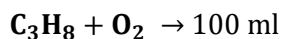
$$\therefore \text{Molar (KE)}_X = \text{Molar (KE)}_Y.$$

$$\therefore \text{(D) is correct.}$$

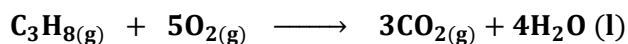
10. Ans. (A,B,C)

$$V_C = 3b = 3 \times \frac{16}{3} \pi r^3 = \frac{48}{3} \pi r^3 \times N_A$$

Theoretical fact of Andrew's Isotherm.

11. Ans. (A, B)

Case-I :-

Let assume C_3H_8 is L.R.

initial	V_1	V_2	
final	0	$V_2 - 5V_1$	$3V_1$

$$\text{Vol. contraction} = V_i - V_f$$

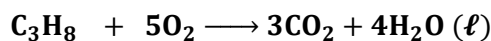
$$V_C = (V_1 + V_2) - (V_2 - 5V_1 + 3V_1)$$

$$45 = 3V_1$$

$$V_1 = 15 \text{ ml (C}_3\text{H}_8\text{)}$$

$$V_2 = 85 \text{ ml (O}_2\text{)}$$

Case-II :-

Let assume O_2 is L.R.

Initial	V_1	V_2	
final	$V_1 - \frac{V_2}{5}$	0	$\frac{3}{5}V_2$

$$\text{Vol. contraction} = V_i + V_f$$

$$V_C = (V_1 + V_2) - \left(V_1 - \frac{V_2}{5} + \frac{3}{5}V_2\right)$$

$$45 = \frac{3}{5}V_2$$

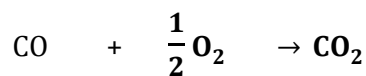
$$V_2 = 75 \text{ ml}$$

$$V_1 = 25 \text{ ml}$$

12. **Ans. (A,B,D)**

$$\text{CO} + \text{CO}_2 = 100 \text{ ml}$$

$$x + y = 100 \text{ ml}$$



$$\text{Initial } x \quad \quad \quad 30$$

$$\text{Final } x - 60 \quad 0 \quad 60$$

Residual gas should be CO = 10 ml

$$\Rightarrow x - 60 = 10$$

$$x = 70 \text{ ml CO}$$

$$y = 30 \text{ ml CO}_2$$

$$\text{absorbed CO}_2 = y + 60 = 90 \text{ ml}$$

13. **Ans. (B)**

$$(P) PV = nRT$$



$P \propto T$, (n & V constant), T increases, P increase



$P = \text{constant}$, T increases, n decreases

$$(Q) \frac{P}{T} = \frac{nR}{V}$$

$$\frac{P^2}{T} = \frac{nR}{V} \cdot P$$

$$A \rightarrow B \quad \quad \quad \frac{P^2}{T} = \text{constant}$$

P increases, n decreases



$P = \text{constant}$

$$\frac{P^2}{T} \text{ increases, n increases}$$

$$(R) T = \frac{PV}{nR}$$



$P = \text{constant}$

T decreases, n increases



$T = \text{constant}$

P increases, n increases

$$(S) P = \frac{nR}{V} \cdot T$$

$$PT = \frac{nR}{V} \cdot T^2$$



$PT = \text{constant}$

T^2 increases, n decreases



$\frac{nR}{V} = \text{constant}$

PT increases, T^2 increases, n constant

14. **Ans. (A)**

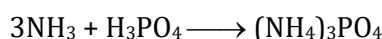
Experimental values only.

15. **Ans. (D)**

Gas having highest a can be liquified easily.

16. **Ans. (A)**

$$T_c = \frac{8a}{27Rb}$$

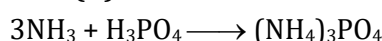
17. **Ans. (D)**

$$n_{\text{NH}_3} = 3n_{\text{H}_3\text{PO}_4}$$

Let x moles of NH_3 is produced

$$\therefore x \times 1 = 0.5 \times \frac{2}{3} \times 3 \Rightarrow x = 1 \text{ mole}$$

$$\therefore \text{CO}_2 = \frac{1}{2} \text{ mole} = 0.50 \text{ mole}$$

18. **Ans. (A)**

$$n_{\text{NH}_3} = 3n_{\text{H}_3\text{PO}_4}$$

Let x moles of NH_3 is produced

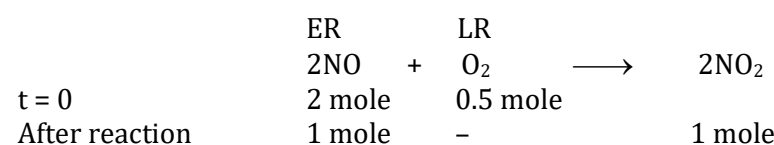
$$\therefore x \times 1 = 0.5 \times \frac{2}{3} \times 3 \Rightarrow x = 1 \text{ mole}$$

$$\therefore \text{CO}_2 = \frac{1}{2} \text{ mole}$$

$$P = \frac{nRT}{V} = \frac{1.5 \times 0.08 \times 300}{36} = 1 \text{ atm}$$

$$\therefore P_{\text{total}} = P_{\text{initial}} + P_{\text{NH}_3 + \text{CO}_2} = 1 + 1 = 2 \text{ atm}$$

$$\therefore \Delta P = 1 \text{ atm} \Rightarrow 760 \text{ mm}$$

19. **Ans. (2.00)**

$$n_i = 2.5 \text{ mole}; n_f = 2 \text{ mole}$$

$$\Delta P = \frac{\Delta nRT}{V} = \frac{0.5 \times R \times T}{V} = \frac{0.5 \times \frac{1}{12} \times 300}{6.25} = 2$$

20. **Ans. (820.00)**

$$P_A = P_B + 100$$

$$P_B = P_{\text{atm}} - 40$$

$$P_B = 720$$

$$P_A = 720 + 100 = 820 \text{ mmHg}$$